

Tutorial 05: June 5

1. Expected Runtime

Give the best-case and expected running time for the following function. You can assume that the Shuffle operation requires $\mathcal{O}(n)$ time and the array A contains no duplicates.

Note: the *Shuffle()* function produces each permutation equally likely.

```
MonkeySort(A)    // A is an array oof n elements
  shuffle(A)
  if A is sorted
    return A
  else
    return MonkeySort(A)
```

2. Recursion Tree Height Analysis

Suppose we have an algorithm as follows, analyze its behaviour and run time. We suppose that array A is sorted. Additionally, Array splitting and printing is done in $O(1)$ time.

```
Partition_and_Find(Array A, size n):
  if (size <= 1) return;
  left = A[0 ... n/2-1];
  right = A[n/2 ... n-1];
  middle = A[n/4 ... 3n/4-1];

  Partition_and_Find(left, n/2);
  Partition_and_Find(middle, n/2);
  Partition_and_Find(right, n/2);

  // bool BinarySearch(Array A, int value);
  result = BinarySearch(A, (A[0]+A[n-1])/2);
  print(result);
  return 0;
```

3. Efficient In-Place Partition (Hoare Partition)

With this question, we will take a look at Hoare Partition and go through an example. Apply following pseudo-code with $A = [8, 17, 10, 1, 6, 20, 9, 2, 13, 7]$ and $p=2$

partition(A, p)

A : array of size n , p : integer s.t. $0 \leq p < n$

1. *swap*($A[n-1], A[p]$)
2. $i \leftarrow -1, j \leftarrow n-1, v \leftarrow A[n-1]$
3. **loop**
4. **do** $i \leftarrow i+1$ **while** $A[i] < v$
5. **do** $j \leftarrow j-1$ **while** $j \geq i$ and $A[j] > v$
6. **if** $i \geq j$ **then break** (goto 9)
7. **else** *swap*($A[i], A[j]$)
8. **end loop**
9. *swap*($A[n-1], A[i]$)
10. **return** i