CS 240: Data Structures and Data Management

Winter 2023

Tutorial 02: January 23

This tutorial focuses on runtime analysis and priority queues. There are 4 questions in total - 2 easy [E], 1 medium [M], and 1 hard [H].

1. [M] Loop Analysis - Iteration

Provide a tight Θ bound on the following pseudocode as a function of n:

Algorithm 1: Iterative Pseudocode

```
1 k \leftarrow 1
{f 2} for i from 1 to n do
        j \leftarrow 0
        while j \leq n \ \mathbf{do}
         j \leftarrow j + k
        end
6
        k \leftarrow 2k
8 end
```

2. [E] Algorithm Design - Heaps

How would you implement a stack using a heap? Analyse the complexity of the push and pop operations.

3. [H] Loop Analysis - Recursion:

Provide a tight O bound for the runtime of the following algorithm. You may assume that at each recursive step, n is an integer.

```
Algorithm 2: Stooge(A, i, j)
```

```
Input: Array A of size n, index i (initially 0), index j (initially n-1)
  Output: No output but the subarray A[i ... j] will be sorted
1 if A[j] < A[i] then
\mathbf{2} \mid \text{SWAP}(A[i], A[j])
3 end
4 if j - i + 1 > 2 then
      t \leftarrow \left| \frac{j-i+1}{3} \right|;
      STOOGE(A, i, j - t);
6
      STOOGE(A, i + t, j);
      STOOGE(A, i, j - t);
9 end
```

4. [E] Max-Heap Operations:

1. Insert 27 and 9 into the following heap, and then perform a delete-max operation on the resulting heap.

