CS 240E: Structures and Data Management Winter 2021 Tutorial 3: AVL Trees

Warmup (optional). Let T be an AVL tree with n nodes and height h. If N(h) is the minimal number of nodes T can have, then show that  $N(h) \ge 2^{\frac{h}{2}}$ .

1. Give an algorithm for inserting in an AVL-tree that does not have parent references.

**2.** Let a 2-AVL tree be a binary search tree where for every node, the difference of heights of its left and right subtree is at most 2. Prove that a 2-AVL tree has height at most  $3 \log n$  where n is the number of nodes in the tree.