The primary goal of this section is to be able to use linked lists and trees.

Linked lists

Racket's list type is more commonly known as a linked list.

Each node contains an item and a link (pointer) to the next node in the list.

The link in the last node is a sentinel value.

In Racket we use empty, and in C we use a NULL pointer.

Linked lists are usually represented as a link (pointer) to the front.

Unlike arrays, linked list nodes are not arranged sequentially in memory. There is no fast and convenient way to “jump” to the i-th element. The list must be traversed from the front. Traversing a linked list is $O(n)$. 
A significant advantage of a linked list is that its length can easily change, and the length does not need to be known in advance.

The memory for each node is allocated dynamically (i.e., using dynamic memory).

Functional vs. Imperative approach

In Section 03, we discussed some of the differences between the functional and imperative programming paradigms.

The core concept of a linked list data structure is independent of any single paradigm.

However, the approach used to implement linked list functions are often very different.

Programming with linked lists further illustrates the differences between the two paradigms.

Dynamic memory in Racket

Dynamic memory in Racket is mostly “hidden”.

The cons function dynamically creates a new linked list node.

In other words, inside of every cons is a hidden malloc.

Structure constructors also use dynamic memory (e.g., make-posn or simply posn in full Racket).

list and quote list notation '(1 2 3) implicitly use cons.
In the functional programming paradigm, functions always generate new values rather than changing existing ones.

Consider a function that “squares” a list of numbers.

- In the functional paradigm, the function must generate a new list, because there is no mutation.
- In the imperative paradigm, the function is more likely to mutate an existing list instead of generating a new list.

sqr-list uses cons to construct a new list:

```
(define (sqr-list lst)
  (cond [(empty? lst) empty]
        [else (cons (sqr (first lst))
                    (sqr-list (rest lst)))]))
```

```
(define a '(10 3 5 7))
(define b (sqr-list a))
```

Of course, in an imperative language (e.g., C) it is also possible to write a “square list” function that follows the functional paradigm and generates a new list.

This is another example of why clear communication (purposes and contracts) is so important.

In practice, most imperative list functions perform mutation. If the caller wants a new list (instead of mutating an existing one), they can first make a copy of the original list and then mutate the new copy.
Mixing paradigms

Problems may arise if we naïvely use the functional paradigm in an imperative environment without considering the consequences.

This is especially important in C, where there is no garbage collector.

<table>
<thead>
<tr>
<th>Functional (Racket)</th>
<th>Imperative (C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>no mutation</td>
<td>mutation</td>
</tr>
<tr>
<td>garbage collector</td>
<td>no garbage collector</td>
</tr>
<tr>
<td>hidden pointers</td>
<td>explicit pointers</td>
</tr>
</tbody>
</table>

The following example highlights the potential problems.

Consider an insert function (used in insertion sort).

;; (insert n slon) inserts n into a sorted list of numbers

(define (insert n slon)
  (cond [(empty? slon) (cons n empty)]
        [(<= n (first slon)) (cons n slon)]
        [else (cons (first slon) (insert n (rest slon)))]))

(define a '(10 20 50 100))
(define b (insert 30 a))

What will the memory diagram look like for a and b?

The lists share the last two nodes.

example: more node sharing in Racket

(define a '(4 5 6))
(define b (cons 3 a))
(define c (append '(1 2) b))

The lists share the last two nodes.
In Racket, lists can share nodes with no negative consequences. It is \textit{transparent} because there is \textbf{no mutation}, and there is a \textbf{garbage collector}.

In an imperative language like C, this configuration is problematic.

- If we call a mutative function such as “square list” on \(a\), then some of the elements of \(b\) will unexpectedly change.
- If we explicitly \texttt{free} all of the memory for list \(a\), then list \(b\) will become invalid.

To avoid mixing paradigms, we use the following \textit{guidelines} when implementing linked lists in C:

- lists shall not \textbf{share nodes}
- new nodes shall only be created (\texttt{malloc’d}) when necessary (inserting nodes and creating new lists).

In Racket, lists generated with \texttt{cons} are immutable. There is a special \texttt{mcons} function to generate a mutable list.

This is one of the significant differences between the Racket language and the Scheme language.

In the Scheme language, lists generated with \texttt{cons} are mutable.
Linked lists in C

We declare a linked list node (llnode) that stores an "item" and a link (pointer) to the next node. For the last node, next is NULL.

```c
struct llnode {
    int item;
    struct llnode *next;
};
```

A C structure can contain a pointer to its own structure type. This is the first recursive data structure we have seen in C.

There is no “official” way of implementing a linked list in C. The CP:AMA textbook and other sources use slightly different conventions.

In this Section we use a wrapper strategy, where we wrap the link to the first node of a list inside of another structure (llist).

```c
struct llist {
    struct llnode *front;
};
```

This wrapper strategy makes some of the following code more straightforward.

It also makes it easier to avoid having lists share nodes (mixing paradigms).

In an Appendix we present examples that do not use a wrapper and briefly discuss the advantages and disadvantages.

To dynamically create a list, we define a list_create function.

```c
struct llist *list_create(void) {
    struct llist *lst = malloc(sizeof(struct llist));
    lst->front = NULL;
    return lst;
}
```

```c
int main(void) {
    struct llist *lst = list_create();
    // ...
}
```
We need to add items to our linked list.

The following code creates a new node

```c
struct llnode *new_node(int i, struct llnode *pnext) {
    struct llnode *node = malloc(sizeof(struct llnode));
    node->item = i;
    node->next = pnext;
    return node;
}
```

And the following code inserts a new node to the front of the list.

```c
void add_front(int i, struct llist *lst) {
    lst->front = new_node(i, lst->front);
}
```

Traversing a list

We can traverse a list iteratively or recursively.

When iterating through a list, we typically use a (llnode) pointer to keep track of the "current" node.

```c
int length(const struct llist *lst) {
    int len = 0;
    struct llnode *node = lst->front;
    while (node) {
        ++len;
        node = node->next;
    }
    return len;
}
```

Remember (node) will be false at the end of the list (NULL).

When using recursion, remember to recurse on a node (llnode) not the wrapper list itself (llist).

```c
int length_nodes(struct llnode *node, int sofar) {
    if (node == NULL) {
        return sofar;
    }
    return length_nodes(node->next, sofar + 1);
}
```

You can write a corresponding wrapper function:

```c
int list_length(struct llist *lst) {
    return length_nodes(lst->front, 0);
}
```
Destroying a list

In C, we don’t have a *garbage collector*, so we must be able to *free* our linked list. We need to *free* every node and the list wrapper.

When using an iterative approach, we are going to need *two* node pointers to ensure that the nodes are *free*d in a safe way.

```c
void list_destroy(struct llist *lst) {
    struct llnode *curnode = lst->front;
    struct llnode *nextnode = NULL;
    while (curnode) {
        nextnode = curnode->next;
        free(curnode);
        curnode = nextnode;
    }
    free(lst);
}
```

With a recursive approach, it is more convenient to *free* the *rest* of the list before we *free* the first node.

```c
void free_nodes(struct llnode *node) {
    if (node) {
        free_nodes(node->next);
        free(node);
    }
}
void list_destroy(struct llist *lst) {
    free_nodes(lst->front);
    free(lst);
}
```

Duplicating a list

Previously, we used the “square list” function to illustrate the differences between the functional and imperative paradigms.

```c
// list_sqr(lst) squares each item in lst
// effects: modifies lst
void list_sqr(struct llist *lst) {
    struct llnode *node = lst->front;
    while (node) {
        node->item *= node->item;
        node = node->next;
    }
}
```

But what if we do want a *new* list that is squared instead of mutating an existing one?
One solution is to provide a `list_dup` function, that makes a duplicate of an existing list.

The recursive function is the most straightforward:

```c
struct llnode * dup_nodes(struct llnode * oldnode) {
    if (oldnode == NULL) {
        return NULL;
    }
    return new_node(oldnode->item, dup_nodes(oldnode->next));
}

struct llist * list_dup(struct llist * oldlist) {
    struct llist * newlist = list_create();
    newlist->front = dup_nodes(oldlist->front);
    return newlist;
}
```

The iterative solution is more complicated:

```c
struct llist * list_dup(struct llist * oldlist) {
    struct llist * newlist = list_create();
    if (oldlist->front) {
        newlist->front = new_node(oldlist->front->item, NULL);
        struct llnode * oldnode = oldlist->front->next;
        struct llnode * node = newlist->front;
        while (oldnode) {
            node->next = new_node(oldnode->item, NULL);
            node = node->next;
            oldnode = oldnode->next;
        }
    }
    return newlist;
}
```

Imperative insert

Earlier, we saw how the Racket (functional) implementation of `insert` (into a sorted list) would be problematic in C.

For an `insert` function in C, we expect the following behaviour:

```
a: 10 20 50 100
```

```c
insert( 5, a);
insert(30, a);
```

```
a: 5 10 20 30 50 100
```
Removing nodes

In Racket, the `rest` function does not actually remove the first element, instead it provides a pointer to the next node.

In C, we can implement a function that removes the first node.

```c
void remove_front(struct llist *lst) {
    assert(lst->front);
    struct llnode *old_front = lst->front;
    lst->front = lst->front->next;
    free(old_front);
}
```

Removing a node from an arbitrary list position is more complicated.

```c
bool remove_item(int i, struct llist *lst) {
    if (lst->front == NULL) return false;
    if (lst->front->item == i) {
        remove_front(lst);
        return true;
    }
    struct llnode *prevnode = lst->front;
    while (prevnode->next && i != prevnode->next->item) {
        prevnode = prevnode->next;
    }
    if (prevnode->next == NULL) return false;
    struct llnode *old_node = prevnode->next;
    prevnode->next = prevnode->next->next;
    free(old_node);
    return true;
}
```
Revisiting the wrapper approach

Throughout these slides we have used a **wrapper** strategy, where we wrap the link to the first node inside of another structure (llist).

Some of the advantages of this strategy are:

- cleaner function interfaces
- reduced need for double pointers
- reinforces the imperative paradigm
- less susceptible to misuse and list corruption

The disadvantages of the wrapper approach include:

- slightly more awkward recursive implementations
- extra “special case” code around the first item

However, there is one more significant advantage of the wrapper approach: **additional information** can be stored in the list structure.

Consider that we are writing an application where the length of a linked list will be queried often.

Typically, finding the length of a linked list is $O(n)$.

However, we can store (or “cache”) the length in the wrapper structure, so the length can be retrieved in $O(1)$ time.

```c
struct llist {
    struct llnode *front;
    int length;
};
```
Naturally, other list functions would have to update the length as necessary:

- `list_create` would initialize length to zero
- `add_front` would increment length
- `remove_front` would decrement length
- `etc`

**Data integrity**

The introduction of the `length` field to the linked list may seem like a great idea to improve efficiency.

However, it introduces new ways that the structure can be corrupted. What if the `length` field does not accurately reflect the true length?

For example, imagine that someone implements the `remove_item` function, but forgets to update the `length` field?

Or a naïve coder may think that the following statement removes all of the nodes from the list.

```
lst->length = 0;
```

Whenever the same information is stored in more than one way, it is susceptible to *integrity* (consistency) issues.

Advanced testing methods can often find these types of errors, but you must exercise caution.

If data integrity is an issue, it is often better to repack the data structure as a separate ADT module and only provide interface functions to the client.

This is an example of *security* (protecting the client from themselves).
Queue ADT

A queue is like a “lineup”, where new items go to the “back” of the line, and the items are removed from the “front” of the line. While a stack is LIFO, a queue is FIFO (first in, first out).

Typical queue ADT operations:

- add_back: adds an item to the end of the queue
- remove_front: removes the item at the front of the queue
- front: returns the item at the front
- is_empty: determines if the queue is empty

A Stack ADT can be easily implemented using a dynamic array (as we did in Section 10) or with a linked list.

While it is possible to implement a Queue ADT with a dynamic array, the implementation is a bit tricky. Queues are typically implemented with linked lists.

The only concern is that an add_back operation is normally $O(n)$. However, if we maintain a pointer to the back (last element) of the list, in addition to a pointer to the front of the list, we can implement add_back in $O(1)$.

Maintaining a back pointer is a popular modification to a traditional linked list, and another reason to use a wrapper.

```
// queue.h

// all operations are O(1) (except destroy)
struct queue;
struct queue *queue_create(void);
void queue_add_back(int i, struct queue *q);
int queue_remove_front(struct queue *q);
int queue_front(struct queue *q);
bool queue_is_empty(struct queue *q);
void queue_destroy(struct queue *q);
```
struct llnode {
    int item;
    struct llnode *next;
};

struct queue {
    struct llnode *front;
    struct llnode *back; // <-- NEW
};

struct queue *queue_create(void) {
    struct queue *q = malloc(sizeof(struct queue));
    q->front = NULL;
    q->back = NULL;
    return q;
}

void queue_add_back(int i, struct queue *q) {
    struct llnode *node = new_node(i, NULL);
    if (q->front == NULL) {
        q->front = node;
    } else {
        q->back->next = node;
    }
    q->back = node;
}

int queue_remove_front(struct queue *q) {
    assert(q->front);
    int retval = q->front->item;
    struct llnode *old_front = q->front;
    q->front = q->front->next;
    free(old_front);
    if (q->front == NULL) {
        q->back = NULL;
    }
    return retval;
}

The remainder of the Queue ADT is straightforward.

int queue_front(struct queue *q) {
    assert(q->front);
    return q->front->item;
}

bool queue_is_empty(struct queue *q) {
    return q->front == NULL;
}

void queue_destroy(struct queue *q) {
    while (!queue_is_empty(q)) {
        queue_remove_front(q);
    }
    free(q);
}
**Node augmentation strategy**

In a **node augmentation strategy**, each node is augmented to include additional information about the node or the structure.

For example, a **dictionary** node can contain both a *key* (item) and a corresponding *value*.

Or for a **priority queue**, each node can additionally store the priority of the item.

The most common node augmentation for a linked list is to create a **doubly linked list**, where each node also contains a pointer to the *previous* node. When combined with a back pointer in a wrapper, a doubly linked list can add or remove from the front and back in $O(1)$ time.

![Diagram of a doubly linked list]

Many programming environments provide a Double-Ended Queue (deque) ADT, which can be used as a Stack or a Queue ADT.

**Trees**

At the implementation level, **trees** are very similar to linked lists.

Each node can link to more than one node.

![Diagram of a tree structure]
Tree terminology

- The root node has no parent, all others have exactly one.
- Nodes can have multiple children.
- In a binary tree, each node has at most two children.
- A leaf node has no children.
- The height of a tree is the maximum possible number of nodes from the root to a leaf (inclusive).
- The height of an empty tree is zero.
- The number of nodes is known as the node count.

Binary Search Trees (BSTs)

Binary Search Tree (BSTs) enforce the ordering property: for every node with an item $i$, all items in the left child subtree are less than $i$, and all items in the right child subtree are greater than $i$.

Mixing paradigms

As with linked lists, we have to be careful not to mix functional and imperative paradigms, especially when adding nodes. The following example visualizes what Racket returns when a node (45) is added to the BST illustrated earlier.
Our BST node (bstnode) is very similar to our linked list node definition.

```c
struct bstnode {
    int item;
    struct bstnode *left;
    struct bstnode *right;
};

struct bst {
    struct bstnode *root;
};
```

In CS 135, BSTs were used as dictionaries, with each node storing both a key and a value. Traditionally, a BST only stores a single item, and additional values can be added as node augmentations if required.

As with linked lists, we need a function to create a new BST.

```c
// bst_create() creates a new BST
// effects: allocates memory: call bst_destroy

struct bst *bst_create(void) {
    struct bst *t = malloc(sizeof(struct bst));
    t->root = NULL;
    return t;
}
```

Before writing code to insert a new node, first we write a helper to create a new leaf node.

```c
struct bstnode *new_leaf(int i) {
    struct bstnode *leaf = malloc(sizeof(struct bstnode));
    leaf->item = i;
    leaf->left = NULL;
    leaf->right = NULL;
    return leaf;
}
```

As with lists, we can write tree functions recursively or iteratively.
For the recursive version, we will need a wrapper, and we can handle the special case that the tree is empty.

```c
void bst_insert(int i, struct bst *t) {
    if (t->root) {
        insert bstnode(i, t->root);
    } else {
        t->root = new leaf(i);
    }
}
```

For the core function, we recurse on nodes.

```c
void insert bstnode(int i, struct bstnode *node) {
    if (i < node->item) {
        if (node->left) {
            insert bstnode(i, node->left);
        } else {
            node->left = new leaf(i);
        }
    } else if (i > node->item) {
        if (node->right) {
            insert bstnode(i, node->right);
        } else {
            node->right = new leaf(i);
        }
    } // else do nothing, as item already exists
}
```

The iterative version is similar to the linked list approach.

```c
void bst_insert(int i, struct bst *t) {
    struct bstnode *node = t->root;
    struct bstnode *parent = NULL;
    while (node) {
        if (node->item == i) return;
        parent = node;
        if (i < node->item) {
            node = node->left;
        } else {
            node = node->right;
        }
    }
    if (parent == NULL) { // tree was empty
        t->root = new leaf(i);
    } else if (i < parent->item) {
        parent->left = new leaf(i);
    } else {
        parent->right = new leaf(i);
    }
}
```
**Trees and efficiency**

What is the efficiency of bst_insert?

The *worst case* is when the tree is *unbalanced*, and every node in the tree must be visited.

![Tree diagram](image)

In this example, the running time of bst_insert is $O(n)$, where $n$ is the number of nodes in the tree.

The running time of bst_insert is $O(h)$: it depends more on the *height* of the tree ($h$) than the *number of nodes* in the tree ($n$).

The definition of a *balanced tree* is a tree where the height ($h$) is $O(\log n)$.

Conversely, an unbalanced tree is a tree with a height that is *not* $O(\log n)$. The height of an unbalanced tree is $O(n)$.

Using the bst_insert function we provided, inserting the nodes in *sorted order* creates an unbalanced tree.

With a balanced tree, the running time of standard tree functions (e.g., insert, remove, search) are all $O(\log n)$.

With an unbalanced tree, the running time of each function is $O(h)$.

A *self-balancing tree* “re-arranges” the nodes to ensure that tree is always balanced.

With a good self-balancing implementation, all standard tree functions *preserve the balance of the tree* and have an $O(\log n)$ running time.

In CS 240 and CS 341 you will see self-balancing trees.

Self-balancing trees often use node augmentations to store extra information to aid the re-balancing.
Count node augmentation

A popular tree node augmentation is to store in each node the count (number of nodes) in its subtree.

```c
struct bstnode {
    int item;
    struct bstnode *left;
    struct bstnode *right;
    int count;  // *****NEW
};
```

This augmentation allows us to retrieve the number of nodes in the tree in $O(1)$ time.

It also allows us to implement a select function in $O(h)$ time. select(k) finds item with index k in the tree.

The following code illustrates how to select item with index k in a BST with a count node augmentation.

```c
int select_node(int k, struct bstnode *node) {
    assert(node && 0 <= k && k < node->count);
    int left_count = 0;
    if (node->left) left_count = node->left->count;
    if (k < left_count) return select_node(k, node->left);
    if (k == left_count) return node->item;
    return select_node(k - left_count - 1, node->right);
}

int bst_select(int k, struct bst *t) {
    return select_node(k, t->root);
}
```

select(0, t) finds the smallest item in the tree.
Array-based trees

For some types of trees, it is possible to use an array to store a tree.

- the root is stored at a[0]
- for the node at a[i]
  - its left is stored at a[2 * i + 1]
  - its right is stored at a[2 * i + 2]
  - its parent is stored at a[(i - 1) / 2]
- a special sentinel value can be used to indicate an empty node
- a tree of height $h$ requires an array of length $2^h - 1$
  (a dynamic array can be realloc’d as the tree height grows)

Array-based trees are often used to implement “complete trees”, where there are no empty nodes, and every level of the tree is filled (except the bottom).

The heap data structure (not the section of memory) is often implemented as a complete tree in an array.

For self-balancing trees, the self-balancing (e.g., rotations) is often more awkward in the array notation. However, arrays work well with lazy rebalancing, where a rebalancing occurs infrequently (i.e., when a large inbalance is detected). The tree can be rebalanced in $O(n)$ time, typically achieving amortized $O(\log n)$ operations.
Dictionary ADT (revisited)

The dictionary ADT (also called a map, associative array, key-value store or symbol table), is a collection of pairs of keys and values. Each key is unique and has a corresponding value, but more than one key may have the same value.

Typical dictionary ADT operations:

- **lookup**: for a given key, retrieve the corresponding value or “not found”
- **insert**: adds a new key/value pair (or replaces the value of an existing key)
- **remove**: deletes a key and its value

In the following example, we implement a Dictionary ADT using a BST data structure.

As in CS 135, we use int keys and string values.

```c
// dictionary.h
struct dictionary;
struct dictionary *dict_create(void);
void dict_insert(int key, const char *val, struct dictionary *d);
const char *dict_lookup(int key, struct dictionary *d);
void dict_remove(int key, struct dictionary *d);
void dict_destroy(struct dictionary *d);
```

Using the same bstnode structure, we augment each node by adding an additional value field.

```c
struct bstnode {
    int item; // key
    char *value; // additional value (augmentation)
    struct bstnode *left;
    struct bstnode *right;
};
struct dictionary {
    struct bstnode *root;
};
struct dictionary *dict_create(void) {
    struct dictionary *d = malloc(sizeof(struct dictionary));
    d->root = NULL;
    return d;
}
```
When inserting key/value pairs to the dictionary, we make a copy of the string passed by the client. When removing nodes, we also free the value.

If the client tries to insert a duplicate key, we replace the old value with the new value.

First, we will modify the new_leaf function to make a copy of the value provided by the client.

```c
struct bstnode * new_leaf(int key, const char * val) {
    struct bstnode * leaf = malloc(sizeof(struct bstnode));
    leaf->item = key;
    leaf->value = my_strdup(val); // make a copy
    leaf->left = NULL;
    leaf->right = NULL;
    return leaf;
}
```

And the wrapper is essentially the same:

```c
void dict_insert(int key, const char * val, struct dictionary * d) {
    if (d->root) {
        insert_bstnode(key, val, d->root);
    } else {
        d->root = new_leaf(key, val);
    }
}
```

```c
void insert_bstnode(int key, const char * val, struct bstnode * node) {
    if (key == node->item) { // must replace the old value
        free(node->value);
        node->value = my_strdup(val);
    } else if (key < node->item) { // otherwise, it's the same
        if (node->left) {
            insert_bstnode(key, val, node->left);
        } else {
            node->left = new_leaf(key, val);
        }
    } else if (node->right) {
        insert_bstnode(key, val, node->right);
    } else {
        node->right = new_leaf(key, val);
    }
}
```
This implementation of the lookup operation returns NULL if unsuccessful.

```c
const char *dict_lookup(int key, struct dictionary *d) {
    struct bstnode *node = d->root;
    while (node) {
        if (node->item == key) {
            return node->value;
        }
        if (key < node->item) {
            node = node->left;
        } else {
            node = node->right;
        }
    }
    return NULL;
}
```

There are several different ways of removing a node from a BST.

We implement remove with the following strategy:

- A) If the node with the key ("key node") is a leaf, we remove it.
- B) If one child of the key node is empty (NULL), the other child is "promoted" to replace the key node.
- C) Otherwise, we find the node with the next largest key ("next node") in the tree (i.e., the smallest key in the right subtree). We replace the key/value of the key node with the key/value of the next node, and then remove the next node from the right subtree.

```c
void dict_remove(int key, struct dictionary *d) {
    d->root = remove_bstnode(key, d->root);
}
struct bstnode *remove_bstnode(int key, struct bstnode *node) {
    // key did not exist:
    if (node == NULL) return NULL;
    // search for the node that contains the key
    if (key < node->item) {
        node->left = remove_bstnode(key, node->left);
    } else if (key > node->item) {
        node->right = remove_bstnode(key, node->right);
    } else if // continued on next page ...
        // (we have now found the key node)
```
If either child is NULL, the node is removed (free’d) and the other child is promoted.

```c
} else if (node->left == NULL) {
    struct bstnode *new_root = node->right;
    free(node->value);
    free(node);
    return new_root;
} else if (node->right == NULL) {
    struct bstnode *new_root = node->left;
    free(node->value);
    free(node);
    return new_root;
} else // continued...
    // (neither child is NULL)
```

Otherwise, we replace the key/value at this node with next largest key/value, and then remove the next key from the right subtree...

```c
} else {
    // find next largest key and its parent
    struct bstnode *next = node->right;
    struct bstnode *parent_of_next = NULL;
    while (next->left) {
        parent_of_next = next;
        next = next->left;
    }
    // free old value & replace key/value of this node
    free(node->value);
    node->item = next->item;
    node->value = next->value;
    // remove next largest node
    if (parent_of_next) {
        parent_of_next->left = next->right;
    } else {
        node->right = next->right;
    }
    free(next);
    return node;
}
```

Finally, the recursive destroy operation frees the children and the (string) value before itself.

```c
void free_bstnode(struct bstnode *node) {
    if (node) {
        free_bstnode(node->left);
        free_bstnode(node->right);
        free(node->value);
        free(node);
    }
}

void dict_destroy(struct dictionary *d) {
    free_bstnode(d->root);
    free(d);
}
```
**Graphs**

Linked lists and trees can be thought of as “special cases” of a **graph** data structure. Graphs are the only core data structure we are not working with in this course.

Graphs link **nodes** with **edges**. Graphs may be undirected (i) or directed (ii), allow cycles (ii) or be acyclic (iii), and have labeled edges (iv) or unlabeled edges (iii).

**Goals of this Section**

At the end of this section, you should be able to:

- use the new linked list and tree terminology introduced
- use linked lists and trees with a recursive or iterative approach
- use wrapper structures and node augmentations to improve efficiency
- explain why an unbalanced tree can affect the efficiency of tree functions