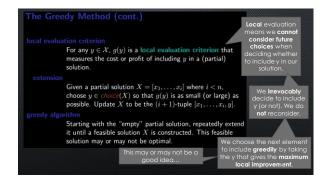


The Greedy Method partial solutions Given a problem instance I, it should be possible to write a feasible solution X as a tuple $[x_1, x_2, \ldots, x_n]$ for some integer n, where $x_i \in \mathcal{X}$ for all i. A tuple $[x_1, \ldots, x_i]$ where i < n is a partial solution if no constraints are violated. Note: it may be the case that a partial solution cannot be extended to a feasible solution.

choice set

For a partial solution $X = [x_1, \ldots, x_i]$ where i < n, we define the choice set $choice(X) = \{y \in \mathcal{X} : [x_1, \ldots, x_i, y] \text{ is a partial solution}\}.$



CORE CHARACTERISTICS Current choice offects (connot undo / change tourent choice offects)

Greedy algorithms do no looking ahead and no backtracking.

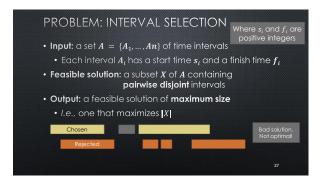
Greedy algorithms can usually be implemented efficiently. Often they consist of a preprocessing step based on the function g, followed by a single pass through the data.

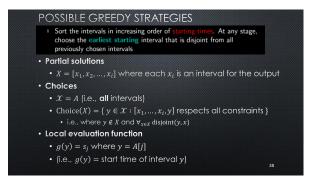
In a greedy algorithm, only one feasible solution is constructed.

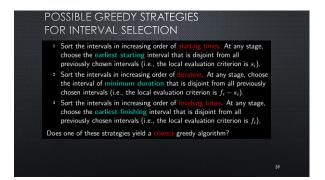
The execution of a greedy algorithm is based on local criteria (i.e., the values of the function g).

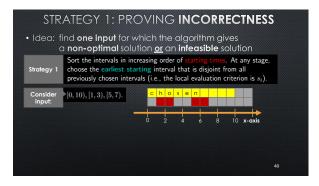
Correctness: For certain greedy algorithms, it is possible to prove that they always yield optimal solutions. However, these proofs can be tricky and complicated!

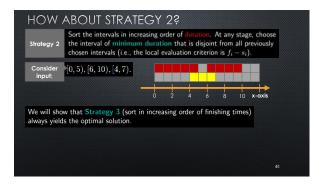






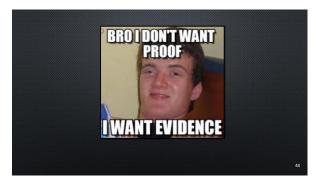












GREEDY CORRECTNESS PROOFS Want to prove: greedy solution X is correct (feasible & optimal) Usually show feasibility directly and optimality by contradiction: Suppose solution 0 is better than X Show this necessarily leads to a contradiction Two broad strategies for deriving this contradiction: Greedy stays ahead: show every choice in X is "at least as good" as the corresponding choice in 0 Exchange: show 0 can be improved by replacing some choice in 0 with a choice in X