# Virtual Memory

## key concepts

virtual memory, physical memory, address translation, MMU, TLB, relocation, paging, segmentation, executable file, swapping, page fault, locality, page replacement

## reading

Three Easy Pieces: Chapters 12-24

## **Physical Memory**

256KB total physical memory

physical address 0x0 physical address 0x3ffff

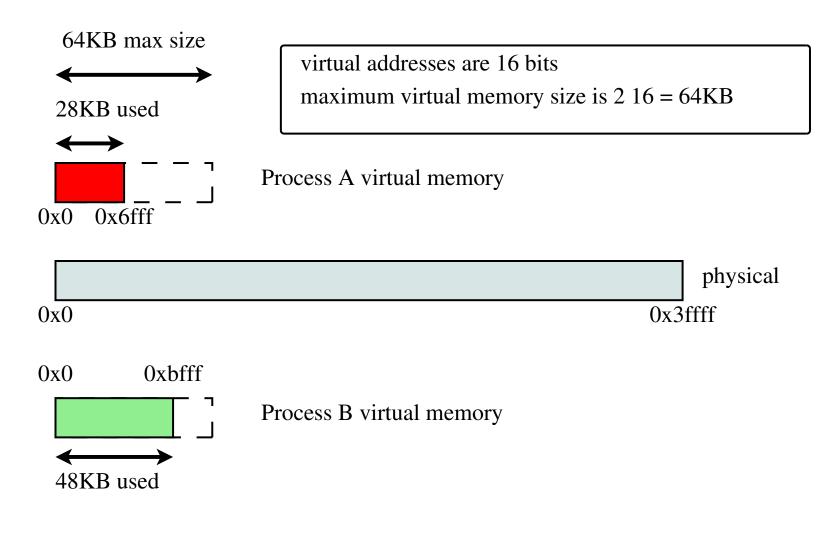
physical addresses are 18 bits

## **Physical Addresses**

• If physical addresses have P bits, the maximum amount of addressable physical memory is  $2^P$  bytes (assuming a byte-addresseable machine).

- Sys/161 MIPS processor uses 32 bit physical addresses  $(P = 32) \Rightarrow$  maximum physical memory size of  $2^{32}$  bytes, or 4GB.
- Larger values of P are common on modern processors, e.g., P=48, which allows 256 TB of physical memory to be addressed.
- The small example on the previous slide uses P = 18
- The actual amount of physical memory on a machine may be less than the maximum amount that can be addressed.

## **Virtual Memory**



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#### Virtual Addresses

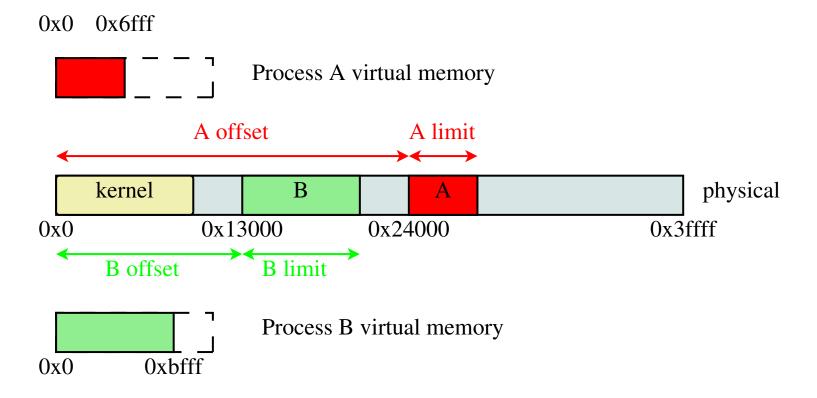
- The kernel provides a separate, private *virtual* memory for each process.
- The virtual memory of a process holds the code, data, and stack for the program that is running in that process.
- If virtual addresses are V bits, the *maximum* size of a virtual memory is  $2^V$  bytes.
  - For the MIPS, V = 32.
  - In our example slides, V = 16.
- Running applications see only virtual addresses, e.g.,
  - program counter and stack pointer hold *virtual addresses* of the next instruction and the stack
  - pointers to variables are virtual addresses
  - jumps/branches refer to *virtual addresses*
- Each process is isolated in its virtual memory, and cannot access other process' virtual memories.

#### **Address Translation**

- Each virtual memory is mapped to a different part of physical memory.
- Since virtual memory is not real, when an process tries to access (load or store) a virtual address, the virtual address is *translated* (mapped) to its corresponding physical address, and the load or store is performed in physical memory.
- Address translation is performed in hardware, using information provided by the kernel.

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## **Dynamic Relocation**



## **Address Translation for Dynamic Relocation**

- CPU includes a memory management unit (MMU), with a a relocation register and a limit register.
  - relocation register holds the physical offset (R) for the running process' virtual memory
  - limit register holds the size L of the running process' virtual memory
- To translate a virtual address v to a physical address p:

```
if v \geq L then generate exception else p \leftarrow v + R
```

- Translation is done in hardware by the MMU
- ullet The kernel maintains a separate R and L for each process, and changes the values in the MMU registers when there is a context switch between processes

## **Properties of Dynamic Relocation**

• Each virtual address space corresponds to a *contiguous range of physical addresses* 

- The kernel is responsible for deciding *where* each virtual address space should map in physical memory
  - The OS must track which parts of physical memory are in use, and which parts are free
  - Since different address spaces may have different sizes, the OS must allocate/deallocate variable-sized chunks of physical memory
  - This creates the potential for *fragmentation* of physical memory

## **Dynamic Relocation Example: Process A**

Limit register: 0x0000 7000 Relocation register: 0x0002 4000

v = 0x102c p = ? v = 0x8800 p = ?v = 0x0000 p = ?

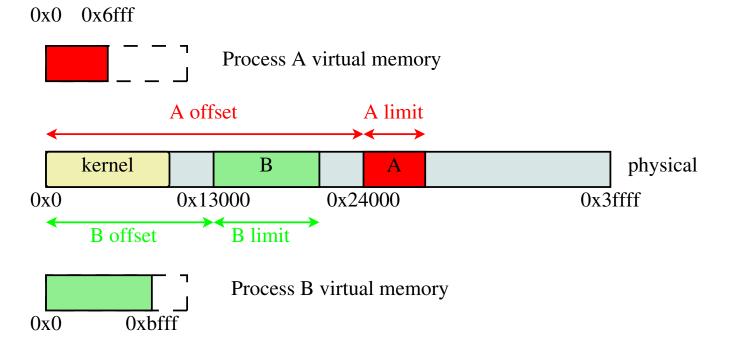
> 0x0 0x6fff Process A virtual memory A offset A limit kernel В physical A 0x13000 0x24000 0x3fffff 0x0B limit **B** offset Process B virtual memory 0x00xbfff

## **Dynamic Relocation Example: Process B**

Limit register: 0x0000 c000 Relocation register: 0x0001 3000

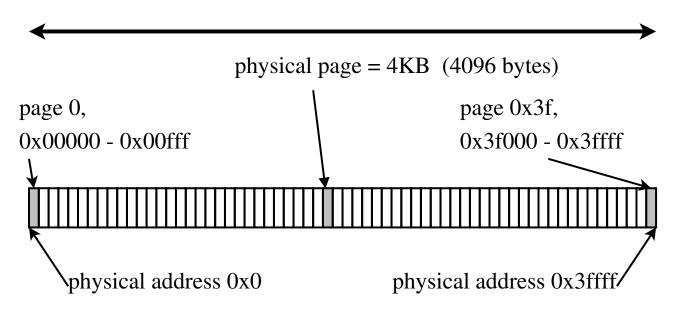
v = 0x102c p = ?v = 0x8800 p = ?

y = 0x0000 p = ?



## **Paging: Physical Memory**

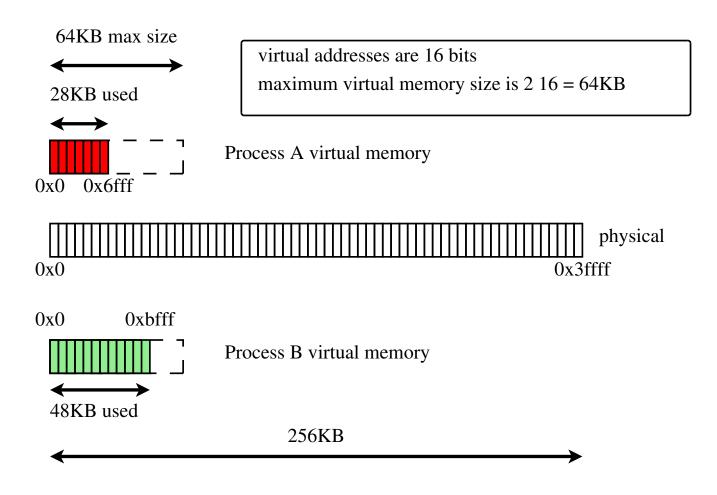
64 physical pages = 256KB total physical memory



physical addresses are 18 bits

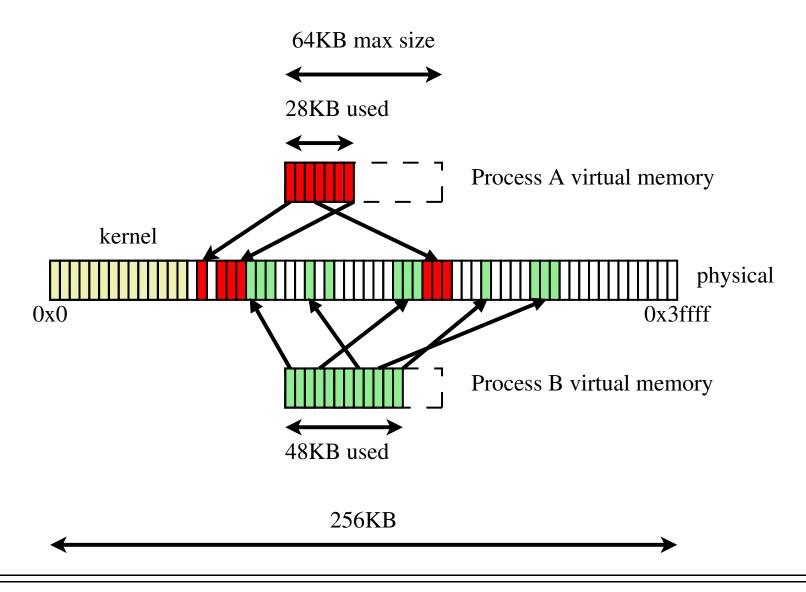
Physical memory is divided into fixed-size chunks called *frames* or *physical* pages. In this example, the frame size is  $2^{12}$  bytes (4KB).

## **Paging: Virtual Memory**



Virtual memories are divided into fixed-size chunks called *pages*. Page size is equal to frame size: 4KB in this example.

## **Paging: Address Translation**



Each page maps to a different frame. Any page can map to any frame.

## **Page Tables**

Process A Page Table

Page	Frame	Valid?	
0x0	0x0f	1	
0x1	0x26	1	
0x2	0x27	1	
0x3	0x28	1	
0x4	0x11	1	
0x5	0x12	1	
0x6	0x13	1	
0x7	0x00	0	
0x8	0x00	0	
0xe	0x00	0	
0xf	0x00	0	

Process B Page Table

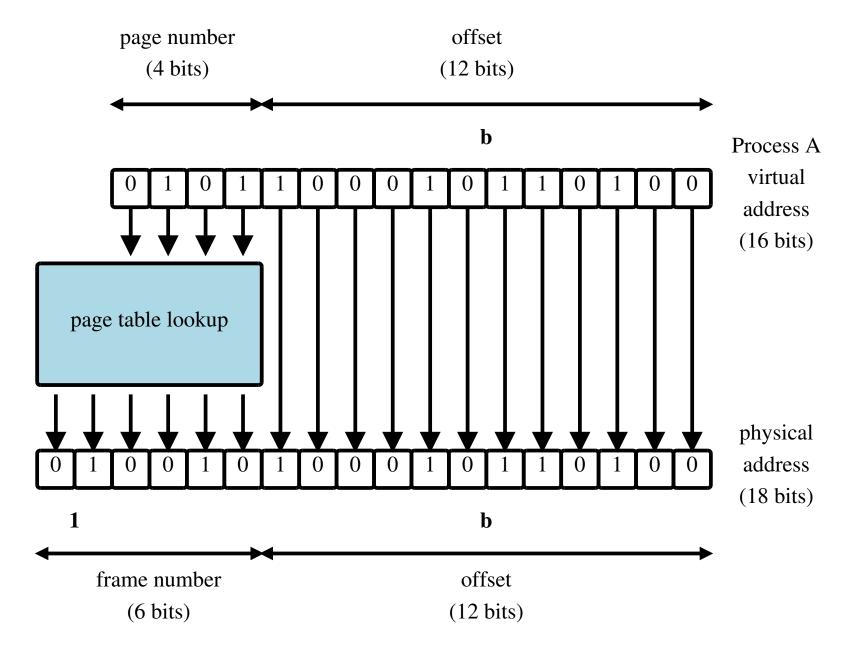
Page	Frame	Valid?	
0x0	0x14	1	
0x1	0x15	1	
0x2	0x16	1	
0x3	0x23	1	
	• • •		
0x9	0x32	1	
0xa	0x33	1	
0xb	0x2c	1	
0xc	0x00	0	
0xd	0x00	0	
0xe	0x00	0	
0xf	0x00	0	

## Address Translation in the MMU, Using Paging

• The MMU includes a *page table base register* which points to the page table for the current process

- How the MMU translates a virtual address:
  - 1. determines the *page number* and *offset* of the virtual address
    - page number is the virtual address divided by the page size
    - offset is the virtual address modulo the page size
  - 2. looks up the page's entry (PTE) in the current process page table, using the page number
  - 3. if the PTE is not valid, raise an exception
  - 4. otherwise, combine page's frame number from the PTE with the offset to determine the physical address
    - physical address is (frame number \* frame size) + offset

### **Address Translation Illustrated**



## **Address Translation Examples (Process A)**

## Process A Page Table

Page	Frame	Valid?	
0x0	0x0f	1	
0x1	0x26	1	
0x2	0x27	1	
0x3	0x28	1	
0x4	0x11	1	
0x5	0x12	1	
0x6	0x13	1	
0x7	0x00	0	
0x8	0x00	0	
• • •	• • •	• • •	
0xe	0x00	0	
Oxf	0x00	0	

$$v = 0x102c p = ?$$

$$v = 0x9800 p = ?$$

$$v = 0x0024 p = ?$$

## **Address Translation Examples (Process B)**

	Page	Frame	Valid?
	0x0	0x14	1
	0x1	0x15	1
	0x2	0x16	1
v = 0x102c p =	0x3	0x23	1
0 0000	•••	• • •	• • •
v = 0x9800 p = ?	0x9	0x32	1
v = 0x0024 p =	0xa	0x33	1
v – 0x0024 p –	0xb	0x2c	1
	0xc	0x00	0
	0xd	0x00	0
	0xe	0x00	0
	0xf	0x00	0

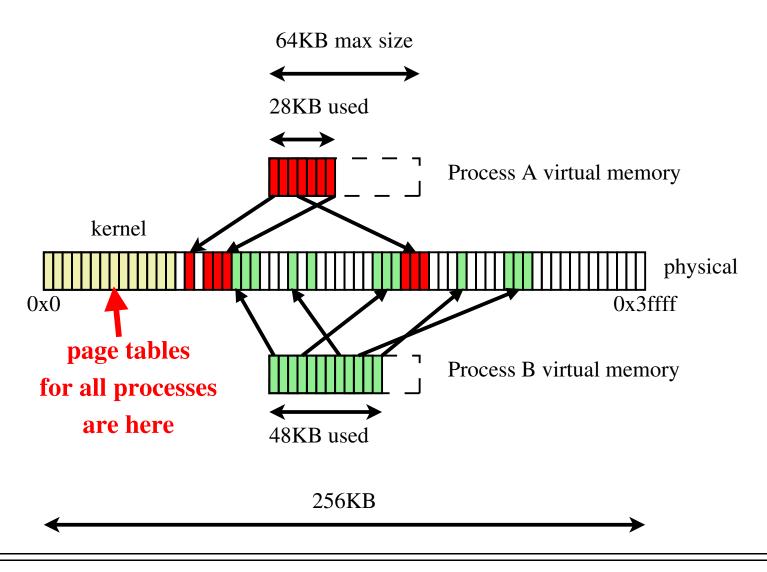
#### **Other Information Found in PTEs**

- PTEs may contain other fields, in addition to the frame number and valid bit
- Example 1: write protection bit
  - can be set by the kernel to indicate that a page is read-only
  - if a write operation (e.g., MIPS lw) uses a virtual address on a read-only page, the MMU will raise an exception when it translates the virtual address
- Example 2: bits to track page usage
  - reference (use) bit: has the process used this page recently?
  - dirty bit: have contents of this page been changed?
  - these bits are set by the MMU, and read by the kernel (more on this later!)

## **Page Tables: How Big?**

- A page table has one PTE for each page in the virtual memory
  - page table size = (number of pages)\*(size of PTE)
  - number of pages = (virtual memory size)/(page size)
- The page table a 64KB virtual memory, with 4KB pages, is 64 bytes, assuming 32 *bits* for each PTE
- Page tables for larger virtual memories are larger (more on this later)

## Page Tables: Where?



Page tables are kernel data structures.

## **Summary: Roles of the Kernel and the MMU**

#### • Kernel:

- Manage MMU registers on address space switches (context switch from thread in one process to thread in a different process)
- Create and manage page tables
- Manage (allocate/deallocate) physical memory
- Handle exceptions raised by the MMU

### • MMU (hardware):

- Translate virtual addresses to physical addresses
- Check for and raise exceptions when necessary

#### **TLBs**

• Execution of each machine instruction may involve one, two or more memory operations

- one to fetch instruction
- one or more for instruction operands
- Address translation through a page table adds one extra memory operation (for page table entry lookup) for each memory operation performed during instruction execution.
- This can be slow!
- Solution: include a Translation Lookaside Buffer (TLB) in the MMU
  - TLB is a small, fast, dedicated cache of address translations, in the MMU
  - Each TLB entry stores a (page# → frame#) mapping

#### **TLB Use**

• What the MMU does to translate a virtual address on page p:

```
if there is an entry (p,f) in the TLB then
  return f    /* TLB hit! */
else
  find p's frame number (f) from the page table
  add (p,f) to the TLB, evicting another entry if full
  return f    /* TLB miss */
```

• If the MMU cannot distinguish TLB entries from different address spaces, then the kernel must clear or invalidate the TLB on each context switch from one process to another.

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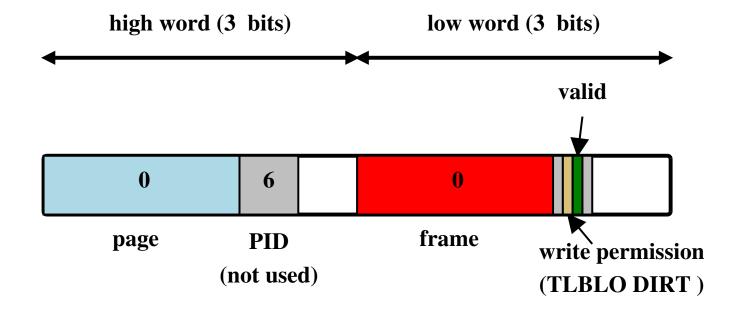
## **Software-Managed TLBs**

- The TLB described on the previous slide is a *hardware-managed TLB* 
  - the MMU handles TLB misses, including page table lookup and replacement of TLB entries
  - MMU must understand the kernel's page table format
- The MIPS has a *software-managed TLB*, which translates a virtual address on page p like this:

```
if there is an entry (p,f) in the TLB then
  return f     /* TLB hit! */
else
  raise exception /* TLB miss */
```

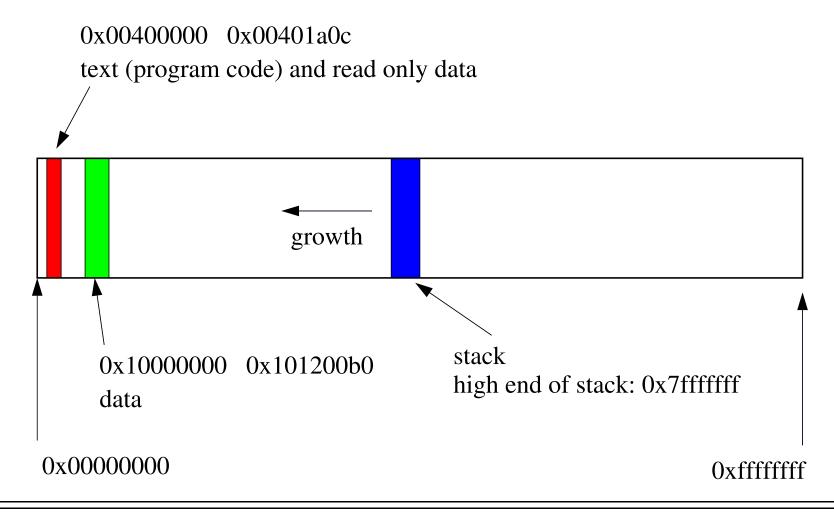
- In case of a TLB miss, the kernel must
  - 1. determine the frame number for p
  - 2. add (p, f) to the TLB, evicting another entry if necessary
- After the miss is handled, the instruction that caused the exception is re-tried

#### The MIPS R3000 TLB



The MIPS TLB has room for 64 entries. Each entry is 64 bits (8 bytes) long, as shown. See kern/arch/mips/include/tlb.h

## **A More Realistic Virtual Memory**



This diagram illustrates the layout of the virtual address space for the OS/161 test application user/testbin/sort

## Large, Sparse Virtual Memories

- Virtual memory may be large
  - MIPS: V = 32, max virtual memory size is  $2^{32}$  bytes (4 GB)
  - x86-64: V = 48, max virtual memory size is  $2^{48}$  bytes (256 TB)
- Much of the virtual memory may be unused.
  - testbin/sort needs only about 1.2MB of the full 4GB virtual memory it runs in.
- Applicaion may use *discontiguous* segments of the virtual memory
  - In the testbin/sort address space, the data and stack segments are widely spaced. (Why?)

## **Limitations of Simple Address Translation Approaches**

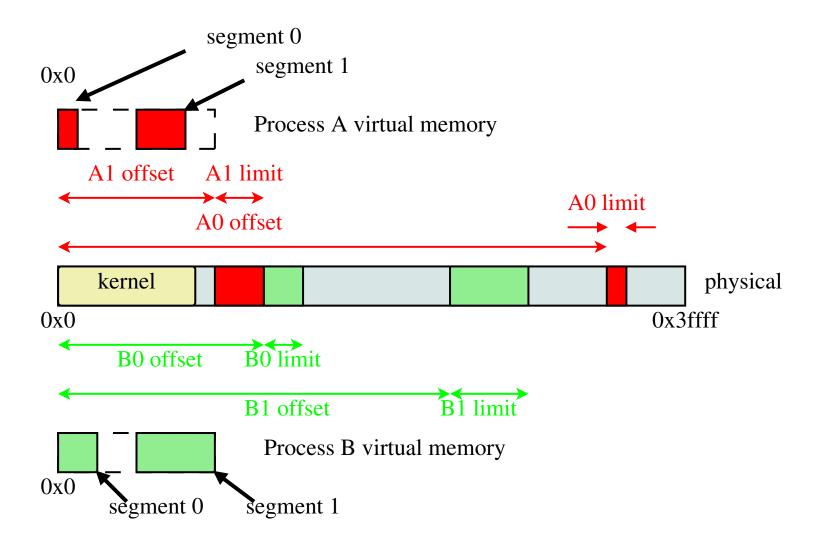
- A kernel that used simple dynamic relocation would have to allocate 2GB of contiguous physical memory for testbin/sort's virtual memory
  - even though sort only uses about 1.2MB
- A kernel that used simple paging would require a page table with  $2^{20}$  PTEs (assuming page size is 4 KB) to map tesbin/sort's address space.
  - this page table is actually larger than the virtual memory that sort needs to use!
  - most of the PTEs are marked as invalid
  - this page table has to be contiguous in kernel memory

## **Segmentation**

• Instead of mapping the entire virtual memory to physical, we can provide a separate mapping for each *segment* of the virtual memory that the application actually uses.

- Instead of a single offset and limit for the entire address space, the kernel maintains an offset and limit for each segment.
  - The MMU has multiple offset and limit registers, one pair for each segment.
- With segmentation, a virtual address can be thought of as having two parts: (segment ID, offset within segment)
- with K bits for the segment ID, we can have up to:
  - $-2^K$  segments
  - $-2^{V-K}$  bytes per segment
- The kernel decides where each segment is placed in physical memory.
  - Fragmentation of physical memory is possible

## **Segmented Address Space Diagram**



### **Translating Segmented Virtual Addresses**

- The MMU needs a relocation register and a limit register for each segment.
  - let  $R_i$  be the relocation offset for the *i*th segment
  - let  $L_i$  be the limit for the *i*th segment
- To translate virtual address v to a physical address p:

```
split p into segment number (s) and address within segment (a) if a \geq L\_s then generate exception else p \leftarrow a + R\_i
```

• As for dynamic relocation, the kernel maintains a separate set of relocation offsets and limits for each process, and changes the values in the MMU's registers when there is a context switch between processes.

## **Segmented Address Translation Example (Process A)**

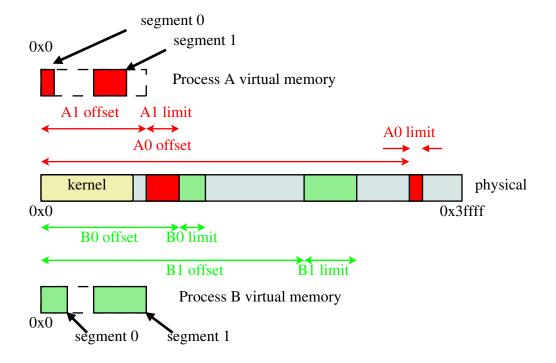
```
Limit Register 0: 0x2000 Relocation Register 0: 0x38000 Limit Register 1: 0x5000 Relocation Register 1: 0x10000
```

```
v = 0x1240 segment=? offset=? p = ?

v = 0xa0a0 segment=? offset=? p = ?

v = 0x66ac segment=? offset=? p = ?

v = 0xe880 segment=? offset=? p = ?
```

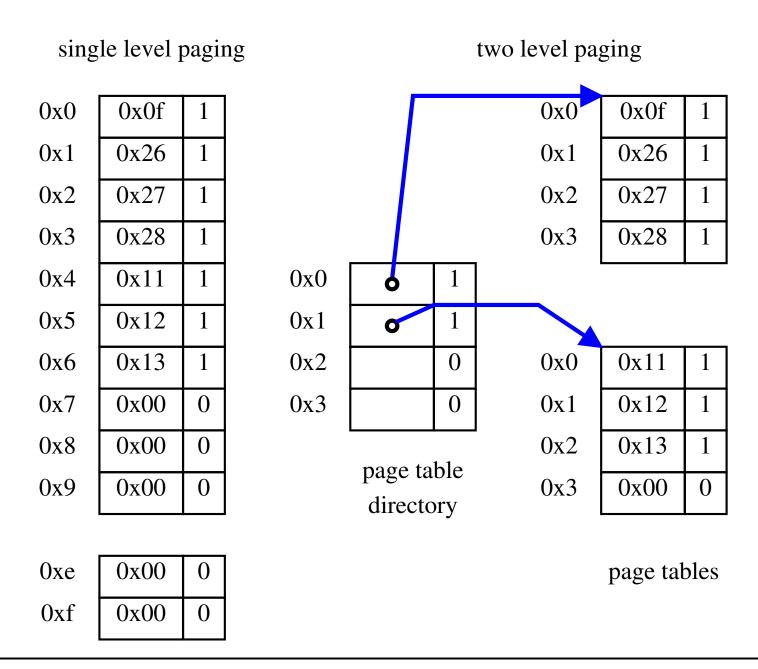


### **Two-Level Paging**

• Instead of having a single page table to map an entire virtual memory, we can split the page table into smaller page tables, and add page table directory.

- instead of one large, contiguous table, we have multiple smaller tables
- if all PTEs in a smaller table are invalid, we can avoid creating that table entirely
- each virtual address has three parts:
  - level one page number: used to index the directory
  - level two page number: used to index a page table
  - offset within the page

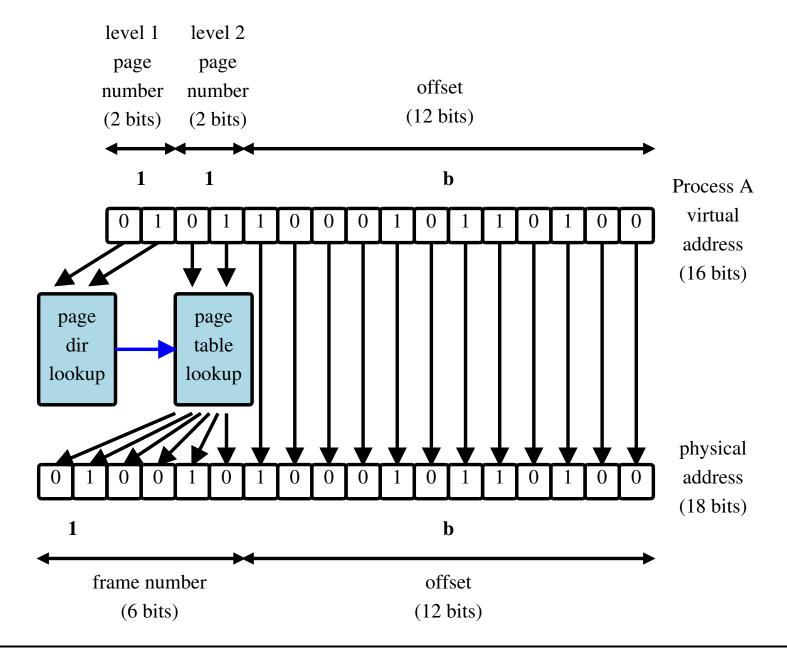
## **Two-Level Paging Example (Process A)**



#### **Address Translation with Two-Level Paging**

- The MMU's *page table base register* points to the page table directory for the current process.
- Each virtual address v has three parts:  $(p_1, p_2, o)$
- How the MMU translates a virtual address:
  - 1. index into the page table directory using  $p_1$  to get a pointer to a 2nd level page table
  - 2. if the directory entry is not valid, raise an exception
  - 3. index into the 2nd level page table using  $p_2$  to find the PTE for the page being accessed
  - 4. if the PTE is not valid, raise an exception
  - 5. otherwise, combine the frame number from the PTE with *o* to determine the physical address (as for single-level paging)

### **Two-Level Address Translation Example**



#### **Limits of Two-Level Paging**

- One goal of two-level paging was to keep individual page tables small.
- Suppose we have 40 bit virtual addresses (V = 40) and that
  - the size of a PTE is 4 bytes
  - page size is 4KB ( $2^{12}$  bytes)
  - we'd like to limit each page table's size to 4KB
- Problem: for large address spaces, we may need a large page table directory!
  - there can be up to  $2^{28}$  pages in a virtual memory
  - a single page table can hold  $2^{10}$  PTEs
  - we may need up to  $2^{18}$  page tables
  - our page table directory will have to have  $2^{18}$  entries
  - if a directory entry is 4 bytes, the directory will occupy 1MB
- this is the problem we were trying to avoid by introducing a second level

### **Multi-Level Paging**

- We can solve the large directory problem by introducing additional levels of directories.
- Example: 4-level paging in x86-64 architecture
- Properties of Multi-Level Paging
  - Can map large virtual memories by adding more levels.
  - Individual page tables/directories can remain small.
  - Can avoid allocating page tables and directories that are not needed for programs that use a small amount of virtual memory.
  - TLB misses become more expensive as the number of levels goes up, since more directories must be accessed to find the correct PTE.

### Virtual Memory in OS/161 on MIPS: dumbvm

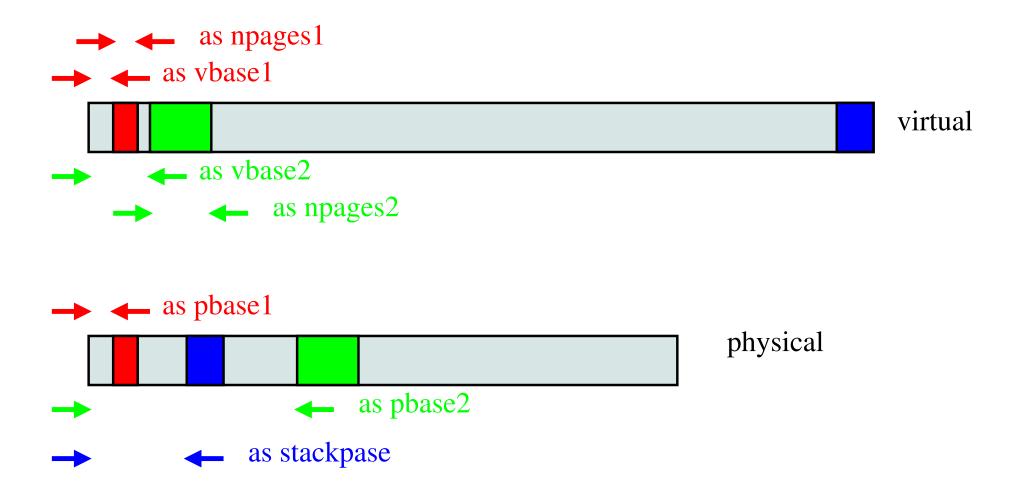
- the MIPS uses 32-bit paged virtual and physical addresses
- the MIPS has a software-managed TLB
  - TLB raises an exception on every TLB miss
  - kernel is free to record page-to-frame mappings however it wants to
- TLB exceptions are handled by a kernel function called vm\_fault
- vm\_fault uses information from an addrspace structure to determine a page-to-frame mapping to load into the TLB
  - there is a separate addrspace structure for each process
  - each addrspace structure describes where its process's pages are stored in physical memory
  - an addrspace structure does the same job as a page table, but the addrspace structure is simpler because OS/161 places all pages of each segment *contiguously* in physical memory

#### The addrspace Stucture

```
struct addrspace {
  vaddr_t as_vbase1; /* base virtual address of code segment */
  paddr_t as_pbase1; /* base physical address of code segment */
  size_t as_npages1; /* size (in pages) of code segment */
  vaddr_t as_vbase2; /* base virtual address of data segment */
  paddr_t as_pbase2; /* base physical address of data segment */
  size_t as_npages2; /* size (in pages) of data segment */
  paddr_t as_stackpbase; /* base physical address of stack */
};
```

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### addrspace Diagram



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## **Address Translation: OS/161 dumbvm Example**

• Note: in OS/161 the stack is 12 pages and the page size is 4 KB = 0 x 1000.

Variable/Field	Proce	ess 1	Process 2			
as_vbase1	0x0040	0000	0x0040	0000		
as_pbase1	0x0020	0000	0x0050	0000		
as_npages1	0x0000	0008	0x0000	0002		
as_vbase2	0x1000	0000	0x1000	0000		
as_pbase2	0x0080	0000	0x00A0	0000		
as_npages2	0x0000	0010	0x0000	0008		
as_stackpbase	0x0010	0000	0x00B0	0000		

	Process 1		Process 2	
Virtual addr	0x0040 0004		0x0040 0004	
Physical addr =		?		?
Virtual addr	0x1000 91A4		0x1000 91A4	
Physical addr =		?		?
Virtual addr	0x7FFF 41A4		0x7FFF 41A4	
Physical addr =		?		?
Virtual addr	0x7FFF 32B0		0x2000 41BC	
Physical addr =		?		?

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### **Initializing an Address Space**

• When the kernel creates a process to run a particular program, it must create an address space for the process, and load the program's code and data into that address space

OS/161 *pre-loads* the address space before the program runs. Many other OS load pages *on demand*. (Why?)

- A program's code and data is described in an *executable file*, which is created when the program is compiled and linked
- OS/161 (and some other operating systems) expect executable files to be in ELF (Executable and Linking Format) format
- The OS/161 execv system call re-initializes the address space of a process int execv (const char \*program, char \*\*args)
- The program parameter of the execv system call should be the name of the ELF executable file for the program that is to be loaded into the address space.

#### **ELF Files**

• ELF files contain address space segment descriptions, which are useful to the kernel when it is loading a new address space

- the ELF file identifies the (virtual) address of the program's first instruction
- the ELF file also contains lots of other information (e.g., section descriptors, symbol tables) that is useful to compilers, linkers, debuggers, loaders and other tools used to build programs

#### **Address Space Segments in ELF Files**

- The ELF file contains a header describing the segments and segment *images*.
- Each ELF segment describes a contiguous region of the virtual address space.
- The header includes an entry for each segment which describes:
  - the virtual address of the start of the segment
  - the length of the segment in the virtual address space
  - the location of the start of the segment image in the ELF file (if present)
  - the length of the segment image in the ELF file (if present)
- the image is an exact copy of the binary data that should be loaded into the specified portion of the virtual address space
- the image may be smaller than the address space segment, in which case the rest of the address space segment is expected to be zero-filled

To initialize an address space, the OS/161 kernel copies segment images from the ELF file to the specifed portions of the virtual address space.

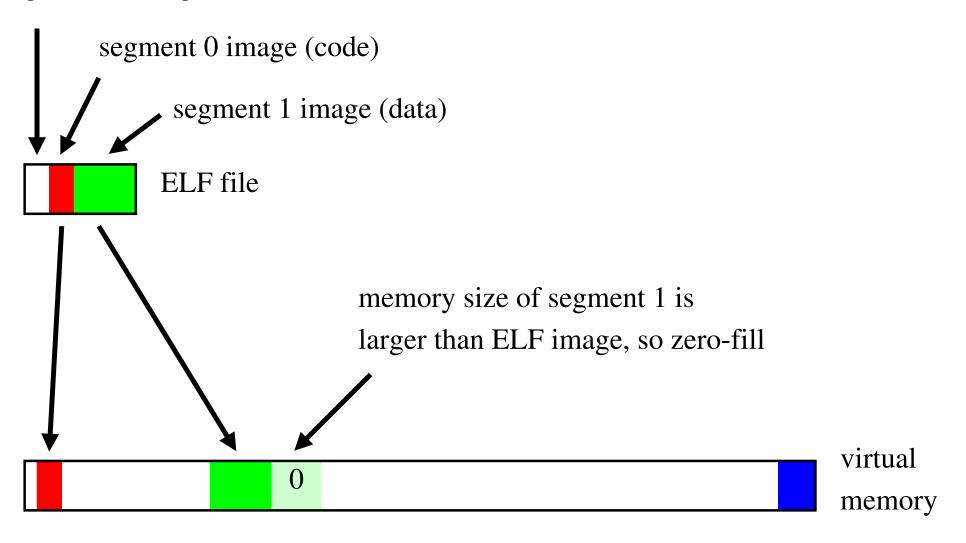
#### **ELF Files and OS/161**

- OS/161's dumbvm implementation assumes that an ELF file contains two segments:
  - a text segment, containing the program code and any read-only data
  - a data segment, containing any other global program data
- the ELF file does not describe the stack (why not?)
- dumbvm creates a *stack segment* for each process. It is 12 pages long, ending at virtual address 0x7fffffff

Look at kern/syscall/loadelf.c to see how OS/161 loads segments from ELF files

## **ELF File Diagram**

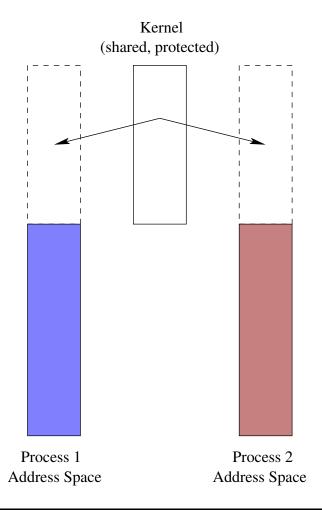
global and segment headers



### Virtual Memory for the Kernel

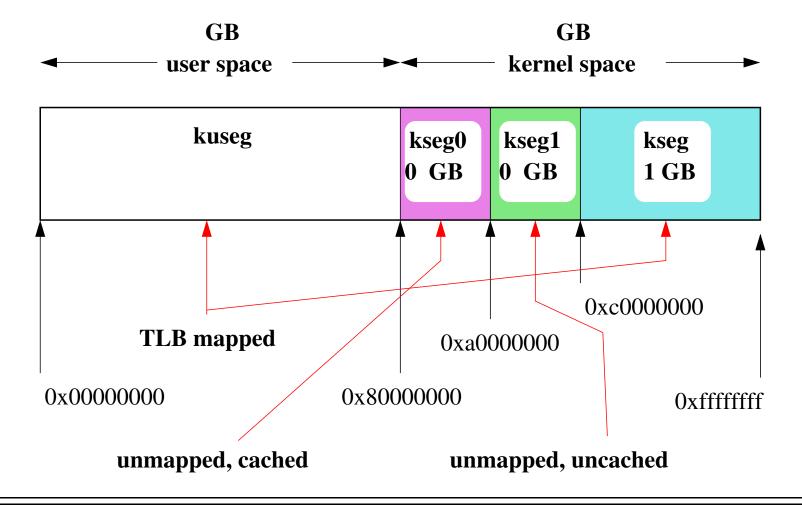
- We would like the kernel to live in virtual memory, but there are some challenges:
  - 1. **Bootstrapping:** Since the kernel helps to implement virtual memory, how can the kernel run in virtual memory when it is just starting?
  - 2. **Sharing:** Sometimes data need to be copied between the kernel and application programs? How can this happen if they are in different virtual address spaces?
- The sharing problem can be addressed by making the kernel's virtual memory *overlap* with process' virtual memories.
- Solutions to the bootstrapping problem are architecture-specific.

#### The Kernel in Process' Address Spaces



Attempts to access kernel code/data in user mode result in memory protection exceptions, not invalid address exceptions.

#### **User Space and Kernel Space on the MIPS R3000**



In OS/161, user programs live in kuseg, kernel code and data structures live in kseg0, devices are accessed through kseg1, and kseg2 is not used.

### **Exploiting Secondary Storage**

#### Goals:

- Allow virtual address spaces that are larger than the physical address space.
- Allow greater multiprogramming levels by using less of the available (primary) memory for each process.

#### **Method:**

- Allow pages from virtual memories to be stored in secondary storage, i.e., on disks or SSDs.
- Swap pages (or segments) between secondary storage and primary memory so that they are in primary memory when they are needed.

#### **Resident Sets and Present Bits**

- When swapping is used, some pages of each virtual memory will be in memory, and others will not be in memory.
  - The set of virtual pages present in physical memory is called the *resident set* of a process.
  - A process's resident set will change over time as pages are swapped in and out of physical memory
- To track which pages are in physical memory, each PTE needs to contain an extra bit, called the *present* bit:
  - valid = 1, present = 1: page is valid and in memory
  - valid = 1, present = 0: page is valid, but not in memory
  - valid = 0, present = x: invalid page

#### **Page Faults**

• When a process tries to access a page that is not in memory, the problem is detected because the page's *present* bit is zero:

- on a machine with a hardware-managed TLB, the MMU detects this when it checks the page's PTE, and generates an exception, which the kernel must handle
- on a machine with a software-managed TLB, the kernel detects the problem when it checks the page's PTE after a TLB miss.
- This event (attempting to access a non-resident page) is called a *page fault*.
- When a page fault happens, it is the kernel's job to:
  - 1. Swap the page into memory from secondary storage, evicting another page from memory if necessary.
  - 2. Update the PTE (set the *present* bit)
  - 3. Return from the exception so that the application can retry the virtual memory access that caused the page fault.

## **Secondary Storage is Slow**

• Access times for disks are measured in *milli*seconds, SSD read latencies are 10's-100's of *micro*seconds.

- Both of these are much higher than memory access times (100's of nanoseconds)
- Suppose that secondary storage access is 1000 times slower than memory access. Then:
  - If there is one page fault every 10 memory accesses (on average), the average memory access time with swapping will be about 100 times larger than it would be without swapping.
  - If there is one page fault every 100 memory accesses (on average), the average memory access time with swapping will be about 10 times larger than it would be without swapping.
  - If there is one page fault every 1000 memory accesses (on average), the average memory access time with swapping will be about 2 times larger than it would be without swapping.

### **Peformance with Swapping**

• To provide good performance for virtual memory accesses, the kernel should try to ensure that page faults are rare.

- Some techniques the kernel can use to improve performance:
  - limit the number of processes, so that there is enough physical memory per process
  - try to be smart about *which* pages are kept in physical memory, and which are evicted.
  - hide latencies, e.g., by *prefetching* pages before a process needs them

## **A Simple Replacement Policy: FIFO**

- replacement policy: when the kernel needs to evict a page from physical memory, which page should it evict?
- the FIFO policy: replace the page that has been in memory the longest
- a three-frame example:

Num	1	2	3	4	5	6	7	8	9	10	11	12
Refs	a	b	c	d	a	b	e	a	b	c	d	e
Frame 1	a	a	a	d	d	d	e	e	e	e	e	e
Frame 2		b	b	b	a	a	a	a	a	c	c	c
Frame 3			c	С	С	b	b	b	b	b	d	d
Fault ?	X	X	X	X	X	X	X			X	X	

## **Optimal Page Replacement**

• There is an optimal page replacement policy for demand paging, called MIN: replace the page that will not be referenced for the longest time.

Num	1	2	3	4	5	6	7	8	9	10	11	12
Refs	a	b	c	d	a	b	e	a	b	c	d	e
Frame 1	a	a	a	a	a	a	a	a	a	c	c	c
Frame 2		b	b	b	b	b	b	b	b	b	d	d
Frame 3			c	d	d	d	e	e	e	e	e	e
Fault ?	X	X	X	X			X			X	X	

• MIN requires knowledge of the future.

#### Locality

• Real programs do not access their virtual memories randomly. Instead, they exhibit *locality*:

- **temporal locality:** programs are more likely to access pages that they have accessed recently than pages that they have not accessed recently.
- spatial locality: programs are likely to access parts of memory that are close to parts of memory they have accessed recently.
- Locality helps the kernel keep page fault rates low.

# Least Recently Used (LRU) Page Replacement

• the same three-frame example:

Num	1	2	3	4	5	6	7	8	9	10	11	12
Refs	a	b	c	d	a	b	e	a	b	c	d	e
Frame 1	a	a	a	d	d	d	e	e	e	c	c	c
Frame 2		b	b	b	a	a	a	a	a	a	d	d
Frame 3			С	c	c	b	b	b	b	b	b	e
Fault ?	X	X	X	X	X	X	X			X	X	X

### **Measuring Memory Accesses**

- The kernel is not aware which pages a program is using unless there is an exception.
- This makes it difficult for the kernel to exploit locality by implementating a replacement policy like LRU.
- The MMU can help solve this problem by tracking page accesses in hardware.
- Simple scheme: add a use bit (or reference bit) to each PTE. This bit:
  - is set by the MMU each time the page is used, i.e., each time the MMU translates a virtual address on that page
  - can be read and cleared by the kernel.
- The use bit provides a small amount of memory usage information that can be exploited by the kernel.

### The Clock Replacement Algorithm

- The clock algorithm (also known as "second chance") is one of the simplest algorithms that exploits the use bit.
- Clock is identical to FIFO, except that a page is "skipped" if its use bit is set.
- The clock algorithm can be visualized as a victim pointer that cycles through the page frames. The pointer moves whenever a replacement is necessary:

```
while use bit of victim is set
   clear use bit of victim
   victim = (victim + 1) % num_frames
choose victim for replacement
victim = (victim + 1) % num_frames
```