1. (10 total marks)

For both parts of this question, use the notation $r_i[x]$ to refer to a read by transaction $T_i$ on object $x$, $w_i[x]$ to refer to a write of $x$ by transaction $T_i$, and $c_i$ to refer to the commit of $T_i$.

a. (5 marks)

Give a simple ($\leq 10$ operations) example of a transaction history that is (conflict) serializable but not recoverable.

\[
\begin{align*}
&w_1[x] \quad r_2[x] \quad c_2 \quad c_1
\end{align*}
\]

b. (5 marks)

Give a simple ($\leq 10$ operations) example of transaction history that is strict but not (conflict) serializable.

\[
\begin{align*}
&r_1[x] \quad w_2[x] \quad w_2[y] \quad c_2 \quad r_1[y] \quad c_1
\end{align*}
\]

2. (12 total marks)

Consider a database containing a relation $R$, which has $T$ tuples and occupies $B$ blocks of space on the disk. There are two B+-tree indexes defined on $R$: a clustered index on attribute $R.a$ and an unclustered index on attribute $R.b$. $R.a$ and $R.b$ are uncorrelated. The following query against $R$ is being executed by the database management system:

\[\text{select } * \text{ from } R \text{ order by } R.b\]

a. (6 marks)

Suppose that the database system’s query plan involves reading $R$ using a sequential scan and then sorting the relation on attribute $R.b$ using an external merge sort. Assume that merge sort operator has sufficient memory to hold only $M$ blocks of data, where $M < B$. What is the I/O cost of this plan, i.e., how many disk block I/O operations will be required to execute the plan? Include both the cost of sequential scan and the cost of the sort.

The sequential scan of $R$ will cost $B$. The merge sort will require $\lceil \log_M B \rceil$ merge passes, each requiring all of the data to be written out and read back in for a total cost of $2B$ per pass. The total cost is:

\[B(1 + 2\lceil \log_M \left\lfloor \frac{B}{M} \right\rfloor )\]

b. (6 marks)

Suppose instead that the database system’s plan is to read $R$’s tuples in sorted order using the unclustered index on $R.b$. Estimate the I/O cost of this plan. Assume that the system has a buffer cache with room for $M$ disk blocks ($M < B$), and that the buffer cache initially contains $M$ of the $B$ blocks of relation $R$.

Without buffering, the index scan would require $T$ I/O operations. With buffering, we can expect that a fraction $M/B$ of the tuples will be found in buffered pages and will not result in I/O operations. Thus, a reasonable cost estimate is:

\[T \left( 1 - \frac{M}{B} \right) \]
3. (12 total marks)

Consider the following query, which is a simplified version of one of the queries from the TPC-H benchmark

```sql
SELECT C.custkey, SUM(L.extendedprice)
FROM customer C, order O, lineitem L, nation N
WHERE C.custkey = O.custkey
    AND L.orderkey = O.orderkey
    AND O.orderdate > DATE('1995-01-01')
    AND L.returnflag = 'R'
    AND C.nationkey = N.nationkey
GROUP BY C.custkey
ORDER BY C.custkey
```

a. (4 marks)

List all of the “interesting orders” that should be considered by a dynamic programming query optimizer as it generates a plan for this query.

- C.custkey and O.custkey
- L.orderkey and O.orderkey
- C.nationkey and N.nationkey

b. (8 marks)

The table below lists some plans that could be considered by a dynamic programming query optimizer as it tries to generate plans for joining the customer and order tables in the query shown above. Suppose that the values in the second column of the table represent the optimizer’s cost estimates for these plans. In the third column of the table, indicate the order, if any, in which the tuples will be produced by this plan. For example, if you believe that the plan will produce output that is ordered on 0.orderdate, write “0.orderdate” in the third column of that plan’s row. If the output tuples will not be sorted on any attribute, write “NONE”. In the fourth column of the table, indicate whether the dynamic programming optimizer would keep the plan or would prune it. If you think that the optimizer would keep the plan, write “KEEP”. If you think that the optimizer would prune the plan, write “PRUNE”.

<table>
<thead>
<tr>
<th>Plan</th>
<th>Cost</th>
<th>Output Order</th>
<th>KEEP/PRUNE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Merge join. One join input is an Index</td>
<td>1000</td>
<td>C,O.custkey</td>
<td>PRUNE</td>
</tr>
<tr>
<td>scan of customer using a clustered index</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>on C.custkey</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>The other input is a sequential scan of</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>order, which is then sorted on</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.custkey using an external merge sort.</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Index nested loop join. Outer input is an</td>
<td>800</td>
<td>C,O.custkey</td>
<td>KEEP</td>
</tr>
<tr>
<td>index scan on customer using a clustered</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>index on C.custkey. Inner input is from an</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>unclustered index on orders on 0.custkey.</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Index nested loop join. Outer input is a</td>
<td>2000</td>
<td>NONE</td>
<td>PRUNE</td>
</tr>
<tr>
<td>sequential scan of customer. Inner input</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>is from an unclustered index on orders on</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.custkey.</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Index nested loop join. Outer input is a</td>
<td>300</td>
<td>NONE</td>
<td>KEEP</td>
</tr>
<tr>
<td>sequential scan of orders. Inner input is</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>from a clustered index on customer on</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>C.custkey.</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
4. (6 total marks)

a. (4 marks)
   Briefly describe one drawback of hash joins relative to nested loop joins. Also, briefly describe
   one drawback of sort-merge joins relative to nested loop joins.

   Hash joins are applicable only to equijoins, while nested loop can be used to implement
   any join. (Most) hash joins are also blocking operations while nested loop joins are
   not. Sort-merge join requires sorted input and is applicable only to equijoins. Nested
   loop join requires no particular tuple input order.

b. (2 marks)
   What does it mean to say that a query execution plan is pipelined? Briefly define this term.
   Operators in pipelined plans produce their output gradually as they consume their
   input, and avoid materializing intermediate results.